1. Bhim and Joe play each other at badminton and for each game, independently of all others, the probability that Bhim loses is 0.2

Find the probability that, in 9 games, Bhim loses
(a) exactly 3 of the games,
(b) fewer than half of the games.

Bhim attends coaching sessions for 2 months. After completing the coaching, the probability that he loses each game, independently of all others, is 0.05

Bhim and Joe agree to play a further 60 games.
(c) Calculate the mean and variance for the number of these 60 games that Bhim loses.
(2)
(d) Using a suitable approximation calculate the probability that Bhim loses more than 4 games.
2. A company has a large number of regular users logging onto its website. On average 4 users every hour fail to connect to the company's website at their first attempt.
(a) Explain why the Poisson distribution may be a suitable model in this case.

Find the probability that, in a randomly chosen 2 hour period,
(b) (i) all users connect at their first attempt,
(ii) at least 4 users fail to connect at their first attempt.

The company suffered from a virus infecting its computer system. During this infection it was found that the number of users failing to connect at their first attempt, over a 12 hour period, was 60 .
(c) Using a suitable approximation, test whether or not the mean number of users per hour who failed to connect at their first attempt had increased. Use a $5 \%$ level of significance and state your hypotheses clearly.
3. A robot is programmed to build cars on a production line. The robot breaks down at random at a rate of once every 20 hours.
(a) Find the probability that it will work continuously for 5 hours without a breakdown.

Find the probability that, in an 8 hour period,
(b) the robot will break down at least once,
(c) there are exactly 2 breakdowns.

In a particular 8 hour period, the robot broke down twice.
(d) Write down the probability that the robot will break down in the following 8 hour period. Give a reason for your answer.
4. A café serves breakfast every morning. Customers arrive for breakfast at random at a rate of 1 every 6 minutes.

Find the probability that
(a) fewer than 9 customers arrive for breakfast on a Monday morning between 10 am and 11 am.

The café serves breakfast every day between 8 am and 12 noon.
(b) Using a suitable approximation, estimate the probability that more than 50 customers arrive for breakfast next Tuesday.
(Total 9 marks)
5. An administrator makes errors in her typing randomly at a rate of 3 errors every 1000 words.
(a) In a document of 2000 words find the probability that the administrator makes 4 or more errors.

The administrator is given an 8000 word report to type and she is told that the report will only be accepted if there are 20 or fewer errors.
(b) Use a suitable approximation to calculate the probability that the report is accepted.
6. A cloth manufacturer knows that faults occur randomly in the production process at a rate of 2 every 15 metres.
(a) Find the probability of exactly 4 faults in a 15 metre length of cloth.
(b) Find the probability of more than 10 faults in 60 metres of cloth.

A retailer buys a large amount of this cloth and sells it in pieces of length $x$ metres. He chooses $x$ so that the probability of no faults in a piece is 0.80
(c) Write down an equation for $x$ and show that $x=1.7$ to 2 significant figures.

The retailer sells 1200 of these pieces of cloth. He makes a profit of 60 p on each piece of cloth that does not contain a fault but a loss of $£ 1.50$ on any pieces that do contain faults.
(d) Find the retailer's expected profit.
7. A botanist is studying the distribution of daisies in a field. The field is divided into a number of equal sized squares. The mean number of daisies per square is assumed to be 3 . The daisies are distributed randomly throughout the field.

Find the probability that, in a randomly chosen square there will be
(a) more than 2 daisies,
(b) either 5 or 6 daisies.

The botanist decides to count the number of daisies, $x$, in each of 80 randomly selected squares within the field. The results are summarised below

$$
\sum x=295 \quad \sum x^{2}=1386
$$

(c) Calculate the mean and the variance of the number of daisies per square for the 80 squares. Give your answers to 2 decimal places.
(d) Explain how the answers from part (c) support the choice of a Poisson distribution as a model.
(e) Using your mean from part (c), estimate the probability that exactly 4 daisies will be found in a randomly selected square.
8. Each cell of a certain animal contains 11000 genes. It is known that each gene has a probability 0.0005 of being damaged.

A cell is chosen at random.
(a) Suggest a suitable model for the distribution of the number of damaged genes in the cell.
(b) Find the mean and variance of the number of damaged genes in the cell.
(c) Using a suitable approximation, find the probability that there are at most 2 damaged genes in the cell.
9. A call centre agent handles telephone calls at a rate of 18 per hour.
(a) Give two reasons to support the use of a Poisson distribution as a suitable model for the number of calls per hour handled by the agent.
(2)
(b) Find the probability that in any randomly selected 15 minute interval the agent handles
(i) exactly 5 calls,
(ii) more than 8 calls.

The agent received some training to increase the number of calls handled per hour. During a randomly selected 30 minute interval after the training the agent handles 14 calls.
(c) Test, at the $5 \%$ level of significance, whether or not there is evidence to support the suggestion that the rate at which the agent handles calls has increased. State your hypotheses clearly.
10. (a) State two conditions under which a Poisson distribution is a suitable model to use in statistical work.

The number of cars passing an observation point in a 10 minute interval is modelled by a Poisson distribution with mean 1.
(b) Find the probability that in a randomly chosen 60 minute period there will be
(i) exactly 4 cars passing the observation point,
(ii) at least 5 cars passing the observation point.
(5)

The number of other vehicles, other than cars, passing the observation point in a 60 minute interval is modelled by a Poisson distribution with mean 12.
(c) Find the probability that exactly 1 vehicle, of any type, passes the observation point in a 10 minute period.
11. An engineering company manufactures an electronic component. At the end of the manufacturing process, each component is checked to see if it is faulty.
Faulty components are detected at a rate of 1.5 per hour.
(a) Suggest a suitable model for the number of faulty components detected per hour.
(b) Describe, in the context of this question, two assumptions you have made in part (a) for this model to be suitable.
(c) Find the probability of 2 faulty components being detected in a 1 hour period.
(d) Find the probability of at least one faulty component being detected in a 3 hour period.
12. (a) Write down the conditions under which the Poisson distribution may be used as an approximation to the Binomial distribution.
(2)

A call centre routes incoming telephone calls to agents who have specialist knowledge to deal with the call. The probability of the caller being connected to the wrong agent is 0.01
(b) Find the probability that 2 consecutive calls will be connected to the wrong agent.
(c) Find the probability that more than 1 call in 5 consecutive calls are connected to the wrong agent.
(3)

The call centre receives 1000 calls each day.
(d) Find the mean and variance of the number of wrongly connected calls.
(3)
(e) Use a Poisson approximation to find, to 3 decimal places, the probability that more than 6 calls each day are connected to the wrong agent.
13. The random variable $J$ has a Poisson distribution with mean 4.
(a) Find $\mathrm{P}(J \geq 10)$.

The random variable $K$ has a binomial distribution with parameters $n=25, p=0.27$.
(b) Find $\mathrm{P}(K \leq 1)$.
(3)
(Total 5 marks)
14. (a) State the condition under which the normal distribution may be used as an approximation to the Poisson distribution.
(b) Explain why a continuity correction must be incorporated when using the normal distribution as an approximation to the Poisson distribution.

A company has yachts that can only be hired for a week at a time. All hiring starts on a Saturday.
During the winter the mean number of yachts hired per week is 5 .
(c) Calculate the probability that fewer than 3 yachts are hired on a particular Saturday in winter.

During the summer the mean number of yachts hired per week increases to 25 .
The company has only 30 yachts for hire.
(d) Using a suitable approximation find the probability that the demand for yachts cannot be met on a particular Saturday in the summer.

In the summer there are 16 Saturdays on which a yacht can be hired.
(e) Estimate the number of Saturdays in the summer that the company will not be able to meet the demand for yachts.
15. An estate agent sells properties at a mean rate of 7 per week.
(a) Suggest a suitable model to represent the number of properties sold in a randomly chosen week. Give two reasons to support your model.
(b) Find the probability that in any randomly chosen week the estate agent sells exactly 5 properties.
(2)
(c) Using a suitable approximation find the probability that during a 24 week period the estate agent sells more than 181 properties.
16. Breakdowns occur on a particular machine at random at a mean rate of 1.25 per week.
(a) Find the probability that fewer than 3 breakdowns occurred in a randomly chosen week.

Over a 4 week period the machine was monitored. During this time there were 11 breakdowns.
(b) Test, at the $5 \%$ level of significance, whether or not there is evidence that the rate of breakdowns has changed over this period. State your hypotheses clearly.
17. A manufacturer produces large quantities of coloured mugs. It is known from previous records that $6 \%$ of the production will be green.

A random sample of 10 mugs was taken from the production line.
(a) Define a suitable distribution to model the number of green mugs in this sample.
(b) Find the probability that there were exactly 3 green mugs in the sample.

A random sample of 125 mugs was taken.
(c) Find the probability that there were between 10 and 13 (inclusive) green mugs in this sample, using
(i) a Poisson approximation,
(ii) a Normal approximation.
(6)
(Total 13 marks)
18. Accidents on a particular stretch of motorway occur at an average rate of 1.5 per week.
(a) Write down a suitable model to represent the number of accidents per week on this stretch of motorway.
(1)

Find the probability that
(b) there will be 2 accidents in the same week,
(c) there is at least one accident per week for 3 consecutive weeks,
(d) there are more than 4 accidents in a 2 week period.
19. The random variable $X \sim \mathrm{~B}(150,0.02)$.

Use a suitable approximation to estimate $\mathrm{P}(X>7)$.
20. The random variable $X$ is the number of misprints per page in the first draft of a novel.
(a) State two conditions under which a Poisson distribution is a suitable model for $X$.

The number of misprints per page has a Poisson distribution with mean 2.5 . Find the probability that
(b) a randomly chosen page has no misprints,
(c) the total number of misprints on 2 randomly chosen pages is more than 7 .

The first chapter contains 20 pages.
(d) Using a suitable approximation find, to 2 decimal places, the probability that the chapter will contain less than 40 misprints.
21. In a manufacturing process, $2 \%$ of the articles produced are defective. A batch of 200 articles is selected.
(a) Giving a justification for your choice, use a suitable approximation to estimate the probability that there are exactly 5 defective articles.
(b) Estimate the probability that there are less than 5 defective articles.
22. The random variables $R, S$ and $T$ are distributed as follows

$$
R \sim \mathrm{~B}(15,0.3), \quad S \sim \operatorname{Po}(7.5), \quad T \sim \mathrm{~N}\left(8,2^{2}\right)
$$

Find
(a) $\mathrm{P}(R=5)$,
(b) $\mathrm{P}(S=5)$,
(c) $\mathrm{P}(T=5)$.
(Total 4 marks)
23. From company records, a manager knows that the probability that a defective article is produced by a particular production line is 0.032 .

A random sample of 10 articles is selected from the production line.
(a) Find the probability that exactly 2 of them are defective.
(3)

On another occasion, a random sample of 100 articles is taken.
(b) Using a suitable approximation, find the probability that fewer than 4 of them are defective.

At a later date, a random sample of 1000 is taken.
(c) Using a suitable approximation, find the probability that more than 42 are defective.
24. Over a long period of time, accidents happened on a stretch of road at random at a rate of 3 per month.

Find the probability that
(a) in a randomly chosen month, more than 4 accidents occurred,
(b) in a three-month period, more than 4 accidents occurred.

At a later date, a speed restriction was introduced on this stretch of road. During a randomly chosen month only one accident occurred.
(c) Test, at the $5 \%$ level of significance, whether or not there is evidence to support the claim that this speed restriction reduced the mean number of road accidents occurring per month.

The speed restriction was kept on this road. Over a two-year period, 55 accidents occurred.
(d) Test, at the $5 \%$ level of significance, whether or not there is now evidence that this speed restriction reduced the mean number of road accidents occurring per month.
25. (a) State two conditions under which a random variable can be modelled by a binomial distribution.

In the production of a certain electronic component it is found that $10 \%$ are defective.
The component is produced in batches of 20 .
(b) Write down a suitable model for the distribution of defective components in a batch.

Find the probability that a batch contains
(c) no defective components,
(d) more than 6 defective components.
(2)
(e) Find the mean and the variance of the defective components in a batch.

A supplier buys 100 components. The supplier will receive a refund if there are more than 15 defective components.
(f) Using a suitable approximation, find the probability that the supplier will receive a refund.
26. (a) Explain what you understand by a critical region of a test statistic.

The number of breakdowns per day in a large fleet of hire cars has a Poisson distribution with mean $\frac{1}{7}$.
(b) Find the probability that on a particular day there are fewer than 2 breakdowns.
(c) Find the probability that during a 14-day period there are at most 4 breakdowns.

The cars are maintained at a garage. The garage introduced a weekly check to try to decrease the number of cars that break down. In a randomly selected 28-day period after the checks are introduced, only 1 hire car broke down.
(d) Test, at the $5 \%$ level of significance, whether or not the mean number of breakdowns has decreased. State your hypotheses clearly.
(Total 15 marks)
27. Minor defects occur in a particular make of carpet at a mean rate of 0.05 per $\mathrm{m}^{2}$.
(a) Suggest a suitable model for the distribution of the number of defects in this make of carpet. Give a reason for your answer.

A carpet fitter has a contract to fit this carpet in a small hotel. The hotel foyer requires $30 \mathrm{~m}^{2}$ of this carpet. Find the probability that the foyer carpet contains
(b) exactly 2 defects,
(3)
(c) more than 5 defects.

The carpet fitter orders a total of $355 \mathrm{~m}^{2}$ of the carpet for the whole hotel.
(d) Using a suitable approximation, find the probability that this total area of carpet contains 22 or more defects.
28. The random variable $R$ has the binomial distribution $\mathrm{B}(12,0.35)$.
(a) Find $\mathrm{P}(R \geq 4)$.

The random variable $S$ has the Poisson distribution with mean 2.71.
(b) Find $\mathrm{P}(S \leq 1)$.

The random variable $T$ has the normal distribution $\mathrm{N}\left(25,5^{2}\right)$.
(c) Find $\mathrm{P}(T \leq 18)$.
(2)
(Total 7 marks)
(6)
(Total 14 marks)
29. (a) Write down two conditions needed to be able to approximate the binomial distribution by the Poisson distribution.

A researcher has suggested that 1 in 150 people is likely to catch a particular virus.
Assuming that a person catching the virus is independent of any other person catching it,
(b) find the probability that in a random sample of 12 people, exactly 2 of them catch the virus.
(c) Estimate the probability that in a random sample of 1200 people fewer than 7 catch the virus.
(Total 10 marks)
30. Vehicles pass a particular point on a road at a rate of 51 vehicles per hour.
(a) Give two reasons to support the use of the Poisson distribution as a suitable model for the number of vehicles passing this point.

Find the probability that in any randomly selected 10 minute interval
(b) exactly 6 cars pass this point,
(c) at least 9 cars pass this point.

After the introduction of a roundabout some distance away from this point it is suggested that the number of vehicles passing it has decreased. During a randomly selected 10 minute interval 4 vehicles pass the point.
(d) Test, at the 5\% level of significance, whether or not there is evidence to support the suggestion that the number of vehicles has decreased. State your hypotheses clearly.
31. (a) Write down the condition needed to approximate a Poisson distribution by a Normal distribution.

The random variable $Y \sim \operatorname{Po}(30)$.
(b) Estimate $\mathrm{P}(Y>28)$.
32. A doctor expects to see, on average, 1 patient per week with a particular disease.
(a) Suggest a suitable model for the distribution of the number of times per week that the doctor sees a patient with the disease. Give a reason for your answer.
(b) Using your model, find the probability that the doctor sees more than 3 patients with the disease in a 4 week period.

The doctor decides to send information to his patients to try to reduce the number of patients he sees with the disease. In the first 6 weeks after the information is sent out, the doctor sees 2 patients with the disease.
(c) Test, at the $5 \%$ level of significance, whether or not there is reason to believe that sending the information has reduced the number of times the doctor sees patients with the disease. State your hypotheses clearly.

Medical research into the nature of the disease discovers that it can be passed from one patient to another.
(d) Explain whether or not this research supports your choice of model. Give a reason for your answer.
33. A botanist suggests that the number of a particular variety of weed growing in a meadow can be modelled by a Poisson distribution.
(a) Write down two conditions that must apply for this model to be applicable.

Assuming this model and a mean of 0.7 weeds per $\mathrm{m}^{2}$, find
(b) the probability that in a randomly chosen plot of size $4 \mathrm{~m}^{2}$ there will be fewer than 3 of these weeds.
(c) Using a suitable approximation, find the probability that in a plot of $100 \mathrm{~m}^{2}$ there will be more than 66 of these weeds.
34. The continuous random variable $X$ represents the error, in mm, made when a machine cuts piping to a target length. The distribution of $X$ is rectangular over the interval $[-5.0,5.0]$.

Find
(a) $\mathrm{P}(X<-4.2)$,
(b) $\mathrm{P}(|X|<1.5)$.

A supervisor checks a random sample of 10 lengths of piping cut by the machine.
(c) Find the probability that more than half of them are within 1.5 cm of the target length.

If $X<-4.2$, the length of piping cannot be used. At the end of each day the supervisor checks a random sample of 60 lengths of piping.
(d) Use a suitable approximation to estimate the probability that no more than 2 of these lengths of piping cannot be used.
35. On a typical weekday morning customers arrive at a village post office independently and at a rate of 3 per 10 minute period.

Find the probability that
(a) at least 4 customers arrive in the next 10 minutes,
(b) no more than 7 customers arrive between 11.00 a.m. and 11.30 a.m.

The period from 11.00 a.m. to 11.30 a.m. next Tuesday morning will be divided into 6 periods of 5 minutes each.
(c) Find the probability that no customers arrive in at most one of these periods.

The post office is open for $3 \frac{1}{2}$ hours on Wednesday mornings.
(d) Using a suitable approximation, estimate the probability that more than 49 customers arrive at the post office next Wednesday morning.

1. (a) Let $X$ be the random variable the number of games Bhim loses. $X \sim \mathrm{~B}(9,0.2)$

$$
\begin{array}{rlrlr}
\mathrm{P}(X \leq 3)-\mathrm{P}(X \leq 2) & =0.9144-0.7382 & \text { or } & (0.2)^{3}(0.8)^{6} \frac{9!}{3!6!} & \text { M1 } \\
& =0.1762 & & =0.1762 & \\
\text { awrt } 0.176 & \text { A1 } & 3
\end{array}
$$

## Note

B1 - writing or use of $\mathrm{B}(9,0.2)$
M1 for writing/ using $\mathrm{P}(X \leq 3)-\mathrm{P}(X \leq 2)$ or $(p)^{3}(1-p)^{6} \frac{9!}{3!6!}$
A1 awrt 0.176
Special case : Use of Po(1.8)
can get B1 M1 A0 - B1 if written $\mathrm{B}(9,0.2)$, M1 for $\frac{\mathrm{e}^{-1.8} 1.8^{3}}{3!}$
or awrt to 0.161
If $\mathrm{B}(9,0.2)$ is not seen then the only mark available for using Poisson is M1.
(b) can get M1 A0 - M1 for writing or using $\mathrm{P}(X \leq 4)$ or may be implied by awrt 0.964
(b) $\mathrm{P}(X \leq 4)=0.9804$

## Note

M1 for writing or using $\mathrm{P}(X \leq 4)$
A1 awrt 0.98
Special case : Use of $\mathbf{P o ( 1 . 8 )}$
can get B1 M1 A0 - B1 if written B(9, 0.2), M1 for $\frac{\mathrm{e}^{-1.8} 1.8^{3}}{3!}$ or awrt to 0.161

If $\mathrm{B}(9,0.2)$ is not seen then the only mark available for using Poisson is M1.
(b) can get M1 A 0 - M1 for writing or using $\mathrm{P}(X \leq 4)$ or may be implied by awrt 0.964
(c) Mean $=3 \quad$ variance $=2.85, \frac{57}{20}$

## Note

B1 3
B1 2.85 , or exact equivalent
(d) $\mathrm{Po}(3)$
poisson
M1
$\mathrm{P}(X>4)=1-\mathrm{P}(X \leq 4) \quad$ M1 $=1-0.8153$ $=0.1847$

A1 3

## Note

M1 for using Poisson
M1 for writing or using $1-\mathrm{P}(X \leq 4) \mathrm{NB} \mathrm{P}(X \leq 4)$ is $0.7254 \mathrm{Po}(3.5)$
and $0.8912 \mathrm{Po}(2.5)$
A1 awrt 0.185
Use of Normal
Can get M0 M1 A0 - for M1 they must write $1-\mathrm{P}(X \leq 4)$ or get awrt 0.187
2. (a) Connecting occurs at random/independently, singly or at a constant rate B1 1

## Note

B1 Any one of randomly/independently/singly/constant rate. Must have context of connection/logging on/fail
(b) $\quad \mathrm{Po}(8)$

B1

## Note

B1 Writing or using $\operatorname{Po}(8)$ in (i) or (ii)
(i) $\mathrm{P}(X=0)=0.0003$

## Note

M1 for writing or finding $\mathrm{P}(X=0)$
A1 awrt 0.0003
(ii) $\mathrm{P}(X \geq 4)=1-\mathrm{P}(X \leq 3)$

$$
\begin{aligned}
& =1-0.0424 \\
& =0.9576
\end{aligned}
$$

A1 5

## Note

M1 for writing or finding $1-\mathrm{P}(X \leq 3)$
A1 awrt 0.958
(c) $\quad \mathrm{H}_{0}: \lambda=4$ (48) $\quad \mathrm{H}_{1}: \lambda>4$ (48)

B1
M1 A1
Method 1
$\mathrm{P}(X \geq 59.5)=\mathrm{P}\left(Z \geq \frac{59.5-48}{\sqrt{48}}\right) \quad \frac{x-0.5-48}{\sqrt{48}}=1.6449 \quad$ M1 M1 A1
$=\mathrm{P}(Z \geq 1.66)$
$=1-0.9515$
$=0.0485 \quad x=59.9$
$0.0485<0.05$
Reject $\mathrm{H}_{0}$. Significant. 60 lies in the Critical region M1
The number of failed connections at the first attempt has increased. A 1 ft

## Note

B1 both hypotheses correct. Must use $\lambda$ or $\mu$
M1 identifying normal
A1 using or seeing mean and variance of 48
These first two marks may be given if the following are seen in the
standardisation formula : 48 and $\sqrt{48}$ or awrt 6.93
M1 for attempting a continuity correction (Method 1: $60 \pm 0.5$ /
Method 2: $x \pm 0.5$ )
M1 for standardising using their mean and their standard deviation and using either Method 1 [59.5, 60 or 60.5. accept $\pm z$.] Method $2[(x \pm 0.5)$ and equal to a $\pm z$ value)
A1 correct $z$ value awrt $\pm 1.66$ or $\pm \frac{59.5-48}{\sqrt{48}}$, or $\frac{x-0.5-48}{\sqrt{48}}=1.6449$
A1 awrt 3 sig fig in range 0.0484 - 0.0485, awrt 59.9
M1 for "reject $\mathrm{H}_{0}$ " or "significant" maybe implied by "correct contextual comment"
If one tail hypotheses given follow through "their prob" and $0.05, p<0.5$
If two tail hypotheses given follow through "their prob" with $0.025, p<0.5$
If one tail hypotheses given follow through "their prob" and $0.95, p>0.5$
If two tail hypotheses given follow through "their prob"
with $0.975, p>0.5$
If no $\mathrm{H}_{1}$ given they get M0
A1 ft correct contextual statement followed through from their prob and $\mathrm{H}_{1}$. need the words number of failed connections/log ons has increased o.e. Allow "there are more failed connections"

NB A correct contextual statement alone followed through
from their prob and $\mathrm{H}_{1}$ gets M1 A1
3. (a) $\quad Y \sim \operatorname{Po}(0.25)$
$\mathrm{P}(Y=0) \quad=\mathrm{e}^{-0.25} \quad$ M1 $=0.7788 \quad \mathrm{~A} 1$

## Note

B1 for seeing or using $\operatorname{Po}(0.25)$
M1 for finding $\mathrm{P}(Y=0)$ either by $\mathrm{e}^{-a}$, where $a$ is positive ( $a$ needn't equal their $\lambda$ ) or using tables if their value of $\lambda$ is in them

Beware common Binomial error using, $p=0.05$ gives 0.7738 but scores B0 M0 A0

A1 awrt 0.779
(b) $\quad X \sim \operatorname{Po}(0.4)$
$\mathrm{P}($ Robot will break down $)=1-\mathrm{P}(X=0)$

$$
\begin{aligned}
& =1-e^{-0.4} \\
& =1-0.067032 \\
& =0.3297
\end{aligned}
$$

M1
A1 3

## Note

B1 for stating or a clear use of $\mathrm{Po}(0.4)$ in part (b) or (c)
M1 for writing or finding $1-\mathrm{P}(X=0)$
A1 awrt 0.33
(c) $\mathrm{P}(X=2) \quad \frac{e^{-0.4}(0.4)^{2}}{2}$

$$
=0.0536
$$

A1 2

## Note

M1 for finding $\mathrm{P}(X=2)$ e.g $\frac{\mathrm{e}^{-\lambda} \lambda^{2}}{2!}$ with their value of $\lambda$ in or if their $\lambda$ is in the table for writing $\mathrm{P}(X \leq 2)-\mathrm{P}(X \leq 1)$

A1 awrt 0.0536
(d) 0.3297 or answer to part (b)

B1ft
B1 dep 2
as Poisson events are independent

## Note

$\mathbf{1}^{\text {st }} \mathbf{B 1}$ their answer to part(b) correct to 2 sf or awrt 0.33
$2^{\text {nd }} \mathbf{B 1}$ need the word independent. This is dependent on them gaining the first B1
SC
Use of Binomial.
Mark parts $a$ and $b$ as scheme. They could get (a)
B0,M0,A0 (b) B0 M1 A0
In part callow M1 for ${ }^{n} C_{2}(p)^{2}(1-p)^{\text {n-2 }}$ with "their n" and "their $p$ ". They could get (c) M1,A0

DO NOT GIVE for $p(x \leq 2)-p(x \leq 1)$
In (d) they can get the first B1 only. They could get (d) B1B0
4. (a) $X \sim \operatorname{Po}(10)$
$\mathrm{P}(X<9) \quad=\mathrm{P}(X \leq 8)$
$=0.3328$

## Note

B1 for using Po(10)
M1 for attempting to find $\mathrm{P}(X \leq 8)$ : useful values
$\mathrm{P}(X \leq 9)$ is $0.4579(\mathrm{M} 0)$, using $\mathrm{Po}(6)$ gives 0.8472 , (M1).
A1 awrt 0.333 but do not accept $\frac{1}{3}$
(b) $\quad Y \sim \operatorname{Po}(40)$

M1 A1
$Y$ is approximately $\mathrm{N}(40,40)$
$\mathrm{P}(Y>50) \quad=1-\mathrm{P}(Y \leq 50)$ M1
$=1-\mathrm{P}\left(\mathrm{Z}<\frac{50.5-40}{\sqrt{40}}\right)$ M1
$=1-\mathrm{P}(Z<1.660 .$. A1
$=1-0.9515$
$=0.0485$
N.B. Calculator gives 0.048437 .

Poisson gives 0.0526 (but scores nothing)

## Note

$\mathbf{1}^{\text {st }} \mathbf{M 1}$ for identifying the normal approximation
$\mathbf{1}^{\text {st }} \mathbf{A 1}$ for [mean $=40$ ] and $[s d=\sqrt{40}$ or var $=40$ ]

## NB These two marks are B1 M1 on ePEN

These first two marks may be given if the following are seen in the standardisation formula : 40 and $\sqrt{40}$ or awrt 6.32
$2^{\text {nd }} \mathbf{M 1}$ for attempting a continuity correction (50 or 30
$\pm 0.5$ is acceptable)
$3^{\text {rd }} \mathbf{M 1}$ for standardising using their mean and their standard deviation and using either $49.5,50$ or 50.5 . (29.5, 30, 30.5) accept $\pm$
$2^{\text {nd }} \mathbf{A 1}$ correct z value awrt $\pm 1.66$ or this may be awarded
if see $\pm \frac{50.5-40}{\sqrt{40}}$ or $\pm \frac{29.5-40}{\sqrt{40}}$
$3^{\text {rd }} \mathbf{A 1}$ awrt 3 sig fig in range $0.0484-0.0485$
5. (a) $X=$ the number of errors in 2000

| words | so |  | $X \sim \operatorname{Po}(6)$ | B1 |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(X \geq 4)=1-\mathrm{P}(X \leq 3)$ |  |  | M1 |  |
|  | $=1-0.1512$ | $=0.8488$ | awrt 0.849 | A1 |

## Note

B1 for seeing or using Po(6)
M1 for $1-\mathrm{P}(X \leq 3)$ or $1-[\mathrm{P}(X=0)$
$+\mathrm{P}(X=1)+\mathrm{P}(X=2)+\mathrm{P}(X=3)]$
A1 awrt 0.849
SC
If $B(2000,0.003)$ is used and leads to awrt 0.849 allow B0 M1 A1

If no distribution indicated awrt 0.8488 scores B1M1A1 but any other awrt 0.849 scores B0M1A1
(b) $\quad Y=$ the number of errors in 8000 words.
$Y \sim \operatorname{Po}(24)$ so use a Normal approx

$$
Y \approx \sim \mathrm{~N}\left(24, \sqrt{24}^{2}\right)
$$

Require $\mathrm{P}(\mathrm{Y} \leq 20)=\mathrm{P}\left(Z<\frac{20.5-24}{\sqrt{24}}\right)$

$$
=\mathrm{P}(Z<-0.714 \ldots)
$$

$$
=1-0.7611 \quad \text { M1 }
$$

$$
=0.2389 \quad \text { awrt }(0.237 \sim 0.239)
$$

[N.B. Exact Po gives 0.242 and no $\pm 0.5$ gives 0.207 ]

## Note

$1^{\text {st }} \mathrm{M} 1$ for identifying the normal approximation
$1^{\text {st }} \mathrm{A} 1$ for [mean $\left.=24\right]$ and $[\mathrm{sd}=\sqrt{24}$ or var $=24]$
These first two marks may be given if the following are seen in the standardisation formula :
$\frac{24}{\sqrt{24}}$ or awrt 4.90
$2^{\text {nd }} \mathrm{M} 1$ for attempting a continuity correction
(20/28 $\pm 0.5$ is acceptable)
$3^{\text {rd }} \mathrm{M} 1$ for standardising using their mean and their standard deviation.
$2^{\text {nd }}$ A1 correct z value awrt $\pm 0.71$ or this may
be awarded if see $\frac{20.5-24}{\sqrt{24}}$ or $\frac{27.5-24}{\sqrt{24}}$
$4^{\text {th }}$ M1 for $1-$ a probability from tables (must have an answer of $<0.5$ )
$3^{\text {rd }} \mathrm{A} 1$ answer awrt 3 sig fig in range $0.237-0.239$
6. (a) $\quad X \sim \operatorname{Po}(2) \quad \mathrm{P}(X=4)=\frac{\mathrm{e}^{-2} \times 2^{4}}{4!}=0.0902 \quad$ awrt $0.09 \quad$ M1

A1 2

## Note

M1 for use of $\operatorname{Po}(2)$ may be implied
A1 awrt 0.09
(b) $\quad Y \sim \operatorname{Po}(8)$

B1
$\mathrm{P}(Y>10)=1-\mathrm{P}(Y \leq 10)=1-0.8159$
$=0.18411 \ldots$
awrt 0.184
M1A1
3

## Note

B1 for $\operatorname{Po}(8)$ seen or used
M1 for $1-\mathrm{P}(Y \leq 10)$ oe
A1 awrt 0.184
(c) $F=$ no. of faults in a piece of cloth of length $x \quad F \sim \operatorname{Po}\left(x \times \frac{2}{15}\right)$

$$
\begin{array}{lr}
\mathrm{e}^{-\frac{2 x}{15}}=0.80 & \text { M1A1 } \\
5 \ldots, \mathrm{e}^{-\frac{2}{15} \times 1.75}=0.791 \ldots & \text { M1 }
\end{array}
$$

These values are either side of 0.80 therefore $x=1.7$ to 2 sf

## Note

$1^{\text {st }}$ M1 for forming a suitable Poisson
distribution of the form $\mathrm{e}^{-\lambda}=0.8$
$1^{\text {st }} \mathrm{A} 1$ for use of lambda as $\frac{2 x}{15}$
(this may appear after taking logs)
$2^{\text {nd }} \mathrm{M} 1$ for attempt to consider a range of values that will prove 1.7 is correct $\mathbf{O R}$ for use of logs to show lambda $=$..
$2^{\text {nd }} \mathrm{A} 1$ correct solution only. Either get 1.7
from using logs or stating values either side
S.C
for $\mathrm{e}^{-\frac{2}{15} \times 1.7}=0.797 \ldots \approx 0.80 \therefore x=1.7$ to 2 sf
allow 2nd M1A0
(d) Expected number with no faults $=1200 \times 0.8=960 \quad$ M1

Expected number with some faults $=1200 \times 0.2=240$
A1
So expected profit $=960 \times 0.60-240 \times 1.50, \quad=£ 216$
M1 A1 4

## Note

$1^{\text {st }} \mathrm{M} 1$ for one of the following 1200 p or $1200(1-p)$ where $p=0.8$ or $2 / 15$.
$1^{\text {st }} \mathrm{A} 1$ for both expected values being correct or two correct expressions.
$2^{\text {nd }} \mathrm{M} 1$ for an attempt to find expected profit, must consider with and without faults
$2^{\text {nd }}$ A1 correct answer only.
7. (a) The random variable X is the number of daisies in a square. Poisson(3) B1

$$
\begin{array}{rlrl}
1-\mathrm{P}(X \leq 2) & =1-0.4232 & 1-\mathrm{e}^{-3}\left(1+3+\frac{3^{2}}{2!}\right) & \\
& =0.5768 & & \text { M1 } \\
\text { A1 }
\end{array}
$$

(b) $\mathrm{P}(X \leq 6)-\mathrm{P}(X \leq 4)=0.9665-0.8153$ $e^{-3}\left(\frac{3^{5}}{5!}+\frac{3^{6}}{6!}\right) \quad$ M1

$$
=0.1512
$$

A1 2
(c) $\quad \mu=3.69$

B1
$\operatorname{Var}(X)=\frac{1386}{80}-\left(\frac{295}{80}\right)^{2}$ M1

$$
=3.73 / 3.72 / 3.71 \quad \text { accept s }{ }^{2}=3.77 \quad \text { A1 } 3
$$

(d) For a Poisson model, Mean $=$ Variance ; For these data $3.69 \approx 3.73$
$\Rightarrow$ Poisson model
B1 1
(e) $\quad \frac{\mathrm{e}^{-3.6875} 3.6875^{4}}{4!}=0.193$
allow their mean or var M1
Awrt 0.193 or 0.194 A1 ft 2
8. (a) $X \sim \mathrm{~B}(11000,0.0005)$

M1 for Binomial,
A1 fully correct
These cannot be awarded unless seen in part a
(b) $\mathrm{E}(X)=11000 \times 0.0005=5.5$ B1
$\operatorname{Var}(X)=11000 \times 0.0005 \times(1-0.0005)$
$=5.49725$
B1 2
B1 cao
B1 also allow 5.50, 5.497, 5.4973, do not allow 5.5
(c) $\mathrm{X} \sim \operatorname{Po}(5.5)$

M1A1
dM1 A1 4
M1 for Poisson
A1 for using Po (5.5)
M1 this is dependent on the previous M mark.
It is for attempting to find $\mathrm{P}(X \leq 2)$
A1 awrt 0.0884
Correct answer with no working gets full marks
Special case If they use normal approximation they could get M0 A0 M1 A0 if they use 2.5 in their standardisation.

NB exact binomial is 0.0883

B1 B1 They must use calls at least once. Independently and randomly are the same reason.
Award the first B1 if they only gain 1 mark.
Special case if they don't put in the word calls but write two correct statements award B0B1
(b) (i) $\quad \mathrm{X} \sim \operatorname{Po}(4.5) \quad$ used or seen in (i) or (ii) M1
$\mathrm{P}(\mathrm{X}=5)=\mathrm{P}(\mathrm{X} \leq 5)-\mathrm{P}(\mathrm{X} \leq 4) \quad \mathrm{M} 1$
$=0.7029-0.5321$
$=0.1708$
correct answers only score full marks
M1 Po (4.5) may be implied by them using it in their calculations in (i) or (ii)
M 1 for $\mathrm{P}(\mathrm{X}<5)-\mathrm{P}(\mathrm{X}<4)$ or $\frac{\mathrm{e}^{-\lambda} \lambda^{5}}{5!}$
A1 only awrt 0.171
(ii) $\quad \mathrm{P}(\mathrm{X}>8)=1-\mathrm{P}(\mathrm{X} \leq 8)$
$=1-0.9597$
$=0.0403$
correct answers only score full marks
M1 for $1-\mathrm{P}(\mathrm{X} \leq 8)$
A1 only awrt 0.0403
(c) $\mathrm{H}_{0}: \lambda=9(\lambda=18)$
may use $\lambda$ or $\mu$
B1
$\mathrm{H}_{1}: \lambda>9(\lambda>18)$
$X \sim$ Po (9) may be implied
B1

| $\mathrm{P}(X \geq 14)=1-\mathrm{P}(X \leq 13) \quad[\mathrm{P}(X \geq 14)=1-0.9261=0.0739] \quad$ att $\mathrm{P}(X \geq 14)$ | $\mathrm{P}(X \geq 15)$ |
| :--- | :--- | :--- |

$=1-0.9261$
$=0.0739$
$0.0739<0.05$
$\mathrm{P}(X \geq 15)=1-0.9780=0.0220$

Accept $\mathrm{H}_{0}$. or it is not significant or a correct statement in context from their values

There is insufficient evidence to say that the number of calls per hour handled by the agent has increased.

B1 both. Must be one tail test. They may use $\lambda$ or $\mu$ and either 9 or 18 and match H 0 and H 1

M1 Po (9) may be implied by them using it in their calculations.
M1 attempt to find $\mathrm{P}(\mathrm{X} \geq 14)$ eg $1-\mathrm{P}(\mathrm{X}<13)$ or $1-\mathrm{P}(\mathrm{X}<14)$
A1 correct probability or CR
To get the next2 marks the null hypothesis must state or imply that $(\lambda)=9$ or 18

M1 for a correct statement based on their probability or critical region or a correct contextualised statement that implies that.

A1. This depends on their M1 being awarded for accepting H0.
Conclusion in context. Must have calls per hour has not increased.
Or the rate of calls has not increased.
Any statement that has the word calls in and implies the rate not increasing
e.g. no evidence that the rate of calls handled has increased

Saying the number of calls has not increased gains A0 as it does not imply rate NB this is an A mark on EPEN

They may also attempt to find $\mathrm{P}(\mathrm{X}<14)=0.9261$ and compare with 0.95
10. (a) Events occur at a constant rate. any two of the 3

Events occur independently or randomly.
Events occur singly.
B1B1 Need the word events at least once.
Independently and randomly are the same reason.
Award the first B1 if they only gain 1 mark
Special case. If they have 2 of the 3 lines without the word events they get B0 B1
(b) Let $X$ be the random variable the number of cars passing the observation point.
Po(6)
B1
(i) $\mathrm{P}(X \leq 4)-\mathrm{P}(X \leq 3)=0.2851-0.1512$ or $\frac{\mathrm{e}^{-6} 6^{4}}{4!}$ $=0.1339$
(ii) $1-\mathrm{P}(X \leq 4)=1-0.2851$ or $1-\mathrm{e}^{-6}\left(\frac{6^{4}}{4!}+\frac{6^{3}}{3!}+\frac{6^{2}}{2!}+\frac{6}{1!}+1\right)$ $=0.7149$

B1 Using Po(6) in (i) or (ii)
M1 Attempting to find $\mathrm{P}(X \leq 4)-\mathrm{P}(X \leq 3)$ or $\frac{\mathrm{e}^{-\lambda} \lambda^{4}}{4!}$
A1 awrt 0.134
M1 Attempting to find $1-\mathrm{P}(X \leq 4)$
A1 awrt 0.715
(c) P ( 0 car and 1 others) +P ( 1 cars and 0 other)
$=\mathrm{e}^{-1} \times 2 \mathrm{e}^{-2}+1 \mathrm{e}^{-1} \times \mathrm{e}^{-2}$
$=0.3679 \times 0.2707+0.3674 \times 0.1353$
$=0.0996+0.0498$
$=0.149$
A1 4
alternative
$\mathrm{P}_{\mathrm{o}}(1+2)=\mathrm{P}_{\mathrm{o}}(3) \mathrm{B} 1$
$\mathrm{P}(\mathrm{X}=1)=3 \mathrm{e}^{-3} \mathrm{M} 1 \mathrm{~A} 1$
$=0.149 \mathrm{~A} 1$

B1 Attempting to find both possibilities.
May be implied by doing $\mathrm{e}^{-\lambda_{1}} \times \lambda_{2} \mathrm{e}^{-\lambda_{2}}+\mathrm{e}^{-\lambda_{2}} \times \lambda_{1} \mathrm{e}^{-\lambda_{1}}$ any values of $\lambda_{1}$ and $\lambda_{2}$

M1 finding one pair of form $\mathrm{e}^{-\lambda_{1}} \times \lambda_{2} \mathrm{e}^{-\lambda_{2}}$ any values of $\lambda_{1}$ and $\lambda_{2}$
A1 one pair correct
A1 awrt 0.149
Alternative.
B1 for Po(3)
M1 for attempting to find $\mathrm{P}(X=1)$ with $\mathrm{Po}(3)$
A1 $3 \mathrm{e}^{-3}$
A1 awrt 0.149
11. (a) $X \sim \operatorname{Po~(1.5)~}$
need Po and 1.5 B1 1
(b) Faulty components occur at a constant rate. any two of the 3

Faulty components occur independently or randomly. only need faulty B1
Faulty components occur singly.
once B1 2
(c) $\mathrm{P}(X=2)=\mathrm{P}(X \leq 2)-\mathrm{P}(X \leq 1)$ or $\frac{\mathrm{e}^{-1.5}(1.5)^{2}}{2}$

M1
$=0.8088-0.5578$
$=0.251$
awrt $0.251 \quad$ A1 2
(d) $\quad X \sim \operatorname{Po}(4.5)$
4.5 may be implied B1
$\mathrm{P}(X \geq 1)=1-\mathrm{P}(X=0)$
M1
$=1-\mathrm{e}^{-4.5}$
$=1-0.0111$
$=0.9889$
awrt 0.989 A1 3
12. (a) If $X \sim \mathrm{~B}(n, p)$ and
$n$ is large, $n>50$
B1
$p$ is small, $p<0.2$
B1 2
then $X$ can be approximated by $\operatorname{Po}(n p)$
(b) $\mathrm{P}(2$ consecutive calls $)=0.01^{2}$ M1
$=0.0001$
A1 2
(c) $\quad X \sim \mathrm{~B}(5,0.01)$
may be implied
B1
$\mathrm{P}(X>1)=1-\mathrm{P}(X=1)-\mathrm{P}(X=0)$
M1
$=1-5(0.01)(0.99)^{4}-(0.99)^{5}$
$=1-0.0480298 \ldots-0.95099 \ldots$
$=0.00098$
awrt 0.00098 A1
3
(d) $\quad X \sim \mathrm{~B}(1000,0.01) \quad$ may be implied by correct mean and variance $\quad \mathrm{B} 1$

Mean $=n p=10$
Variance $=n p(1-p)=9.9$
B1
B1
3
(e) $\quad X \sim \operatorname{Po}(10)$
$\mathrm{P}(X>6)=1-\mathrm{P}(X \leq 6)$ M1
$=1-0.1301$
$=0.8699 \quad$ awrt 0.870 A1 2
13.
(a) $\mathrm{P}(J \geq 10)=1-\mathrm{P}(J \leq 9)$
= $1-0.9919$
$=0.0081$
or $=1-\mathrm{P}(J<10)$
implies method
M1 awrt 0.0081
(b) $\mathrm{P}(K \leq 1)=\mathrm{P}(K=0)+\mathrm{P}(K=1)$ both, implied below even with ' 25 ' missing
$=(0.73)^{25}+25(0.73)^{24}(0.27) \quad$ clear attempt at ' 25 ' required awrt 0.0039 implies M
14. (a) $\lambda>10$ or large
$\mu \mathrm{ok}$
B1 1
(b) The Poisson is discrete and the normal is continuous.
(c) Let $Y$ represent the number of yachts hired in winter
$\mathrm{P}(Y<3)=\mathrm{P}(Y \leq 2)$
$\mathrm{P}(Y \leq 2) \& \operatorname{Po}(5)$
M1
$=0.1247$ awrt 0.125
A1 2
(d) Let $X$ represent the number of yachts hired in summer $X \sim \operatorname{Po}(25)$.
$\mathrm{N}(25,25)$ all correct, can be implied by standardisation below B1 $\mathrm{P}(X>30) \approx \mathrm{P}\left(\mathrm{Z}>\frac{30.5-25}{5}\right) \pm$ standardise with $25 \& 5 ; \pm 0.5$ c.c. $\mathrm{M} 1 ; \mathrm{M} 1$
$\approx \mathrm{P}(\mathrm{Z}>1.1)$
‘one minus'
A1
$\approx 1-0.8643$
awrt 0.136
M1
$\approx 0.1357$
A1 6
(e) no. of weeks $=0.1357 \times 16$ $=2.17$ or 2 or 3

| ANS (d) $\times 16$ | M1 |
| ---: | ---: |
| ans $>16$ M0A0 | A1ft | 2

15. Let $X$ represent the number of properties sold in a week
(a) $\quad \therefore X \sim \mathrm{P}_{0}$ (7)

B1 must be in part a

Sales occur independently / randomly, singly, at a constant rate context needed once
(b) $\mathrm{P}(X=5)=\mathrm{P}(X \leq 5)-\mathrm{P}(X \leq 4)$
or $\frac{7^{5} e^{-7}}{5!}$ M1
$=0.3007-0.1730$

$$
=0.1277
$$

A1 2 awrt 0.128
(c) $\quad \mathrm{P}(X>181) \approx \mathrm{P}(Y \geq 181.5)$ where $Y \sim \mathrm{~N}(168,168) \quad \mathrm{N}(168,168) \quad \mathrm{B} 1$
$=P\left(z \geq \frac{181.5-168}{\sqrt{168}}\right)$
$\pm 0.5$ M1
stand with $\mu$ and $\sigma \quad$ M1
Give A1 for 1.04 or correct expression A1
$=\mathrm{P}(\mathrm{z} \geq 1.04)$
$=1-0.8508$
M1
attempt correct area
$1-p$ where $p>0.5$
$=0.1492$
awrt 0.149
16. (a) Let $X$ represent the number of breakdowns in a week.
$\mathrm{X} \sim \mathrm{P}_{\mathrm{o}}$ (1.25)
B1
Implied
$\mathrm{P}(X<3)=\mathrm{P}(0)+\mathrm{P}(1)+\mathrm{P}(2) \quad$ or $\quad \mathrm{P}(\mathrm{X} \leq 2) \quad \mathrm{M} 1$
$=e^{-1.25}\left(1+1.25+\frac{(1.25)^{2}}{2!}\right)$
$=0.868467$
A1 4
awrt 0.868 or 0.8685
(b) $\quad \mathrm{H}_{0}: \quad \lambda=1.25 ; \quad \mathrm{H}_{1}: \lambda \neq 1.25 \quad\left(\right.$ or $\left.\mathrm{H}_{\mathrm{o}}: \lambda=5 ; \quad \mathrm{H}_{1}: \lambda \neq 5\right) \quad \lambda$ or $\mu \quad$ B1 B1

Let $Y$ represent the number of breakdowns in 4 weeks
Under $\mathrm{H}_{0}, Y \sim \mathrm{P}_{0}(5)$
B1
may be implied

| $\mathrm{P}(Y \geq 11)=$ |
| :---: |
| $\begin{array}{l}\text { One needed for } M\end{array} \quad$ or $\quad \mathrm{P}(Y \leq 10) \quad \mathrm{M} 1$ |

$\mathrm{P}(X \geq 10)=0.0318$
$=0.0137 \quad$ CR $X \geq 11$
A1
$0.0137<0.025,0.0274<0.05,0.9863>0.975,0.9726>0.95$ or $11 \geq 11 \mathrm{M} 1$ any .allow \%
ft from $H_{1}$
Evidence that the rate of breakdowns has changed / decreased
B1ft 7
Context
From their $p$
17. (a) Binomial

B1 1
Let $X$ represent the number of green mugs in a sample
(b) $\quad X \sim B(10,0.06)$

B1
may be implied or seen in part a
$\mathrm{P}(X=3)={ }^{10} \mathrm{C}_{3}(0.06)^{3}(0.94)^{7}$
M1
${ }^{10} C_{3}(\mathrm{p})^{3}(l-\mathrm{p})^{7}$
0.016808....
awrt 0.0168
(c) Let $X$ represent number of green mugs in a sample of size 125
(i) $\mathrm{X} \sim \mathrm{P}_{0}(125 \times 0.06=7.5) \quad$ may be implied B1
$(10 \leq X \leq 13)=\mathrm{P}(X \leq 13)-\mathrm{P}(\mathrm{X} \leq 9) \quad \mathrm{M} 1$
$0.9784-0.7764$
$=0.2020$
awrt 0.202
(ii) $\mathrm{P}(10 \leq X \leq 13) \approx \mathrm{P}(9.5 \leq Y \leq 13.5) \quad$ where $\mathrm{Y} \cup \mathrm{N}(7.5,7.05)$ 7.05 B1
$9.5,13.5 \quad$ B1
$=P\left(\frac{9.5-7.5}{\sqrt{7.05}} \leq z \leq \frac{13.5-7.5}{\sqrt{7.05}}\right)$
$\pm 0.5$ M1
stand. M1
both values or both correct expressions.
$=\mathrm{P}(0.75 \leq \mathrm{z} \leq 2.26)$
awrt 0.75 and 2.26 $\quad$ A1 $\begin{aligned} & \text { A1 } \\ & =0.2147 \\ & \\ & \text { awrt } 0.214 \text { or } 0.215\end{aligned} \quad$ A1 $\begin{aligned} & 6\end{aligned}$
18. (a) Let $X$ be the random variable the no. of accidents per week

$$
X \sim \operatorname{Po}(1.5)
$$

need poisson and $\lambda$ must be in part (a) B1
1
(b) $\mathrm{P}(X=2)=\frac{e^{-1.5} 1.5^{2}}{2}$

$$
\begin{array}{r}
\frac{e^{\mu} \mu^{2}}{2} \text { or } \mathrm{P}(\mathrm{X} \leq 2)-\mathrm{P}(\mathrm{X} \leq 1) \quad \mathrm{M} 1 \\
\text { awrt } 0.251 \quad \mathrm{~A} 1
\end{array}
$$

(c) $\quad \mathrm{P}(\mathrm{X} \geq 1)=1-\quad \mathrm{P}(X=0)=1-e^{-1.5}$
correct exp awrt 0.777 B1

$$
=0.7769
$$

P (at least 1 accident per week for 3 weeks)

$$
\begin{aligned}
& =0.7769^{3} \\
& =0.4689
\end{aligned}
$$

The 0.7769 may be implied
(d) $\quad X \sim \operatorname{Po}(3)$

$$
\begin{aligned}
& \mathrm{P}(X>4)=1-\mathrm{P}(X \leq 4) \\
& =0.1847
\end{aligned}
$$

19. $X=\operatorname{Po}(150 \times 0.02)=\operatorname{Po}(3)$

$$
P(X>7)=1-P(X \leq 7)
$$

$$
=0.0119
$$

Use of normal approximation max awards B0 B0 M1 A0 in the use $1-\mathrm{p}(x<7.5)$
B1, B1(dep)
M1
awrt 0.0119 A1

$$
\begin{aligned}
& z=\frac{7.5-3}{\sqrt{2.94}}=2.62 \\
& p(x>7)=1-p(x<7.5) \\
& =1-0.9953 \\
& =0.0047
\end{aligned}
$$

20. (a) Misprints are random / independent, occur singly B1, B1 2 in space and at a constant rate

Context, any 2
(b) $\mathrm{P}(\mathrm{X}=0)=\mathrm{e}^{-2.5}$
Po (2.5)

$$
=0.08208 \ldots \ldots=0.0821
$$

A1 2
(c) $\mathrm{Y} \sim \operatorname{Po}(5)$ for 2 pages

B1
Implied

$$
\begin{array}{cc}
\mathrm{P}(\mathrm{Y}>7)=1-\mathrm{P}(\mathrm{X} \leq 7) & \mathrm{M} 1 \\
\text { Use of } 1-\text { and correct inequality } &
\end{array}
$$

$$
=1-0.8666=0.1334
$$

$$
\begin{array}{lr}
\text { (d) } & \text { For 20 pages, } \mathrm{Y} \sim \mathrm{P}_{0}(50) \\
\mathrm{Y} \sim \mathrm{~N}(50,50) \text { approx } & \mathrm{B} 1 \\
\mathrm{P}(\mathrm{Y}<40)=\mathrm{P}(\mathrm{Y} \leq 39.5) & \mathrm{B} 1 \\
c c \pm 0.5 & \\
& \\
=\mathrm{P}\left(Z \leq \frac{39.5-50}{\sqrt{50}}\right) & \mathrm{M} 1 \\
\text { standardise above } & \mathrm{A} 1 \\
\text { all correct } & \mathrm{A} 1 \\
=\mathrm{P}(\mathrm{Z} \leq-1.4849) & \mathrm{A} 1 \\
\quad \text { awrt }-1.48 &
\end{array}
$$

21. (a) $\mathrm{X} \sim \mathrm{B}(200,0.02)$

B1
Implied
n large, P small so $\mathrm{X} \sim \mathrm{Po}(\mathrm{np})=\mathrm{Po}(4)$
B1, B1
conditions, $P_{0}(4)$
$\mathrm{P}(\mathrm{X}=5)=\frac{e^{-4} 4^{5}}{5!}$ M1
$P(X \leq 5)-P(X \leq 4)$
$=0.1563$
(b) $\quad \mathrm{P}(\mathrm{X}<5)=\mathrm{P}(\mathrm{X} \leq 4)$

M1

$$
P(X \leq 4)
$$

$=0.6288$
A1 2
[7]
22. (a) $\mathrm{P}(\mathrm{R}=5)=\mathrm{P}(\mathrm{R} \leq 5)-\mathrm{P}(\mathrm{R} \leq 4)=0.7216-0.5155$

Can be implied
$=0.2061$
A1 2
Answer 0.2061
(OR: ${ }_{5}^{15} \mathrm{C}(0.3)^{5}(0.7)^{10}=0.206130 \ldots$ )
(b) $\mathrm{P}(\mathrm{S}=5)=0.2414-0.1321=0.1093$
B1 1
Accept 0.1093 (AWRT) or 0.1094 (AWRT)
(OR: $\frac{7.5^{5} e^{-7.5}}{5!}=0.10937459 \ldots$ )
(c) $\quad \mathrm{P}(\mathrm{T}=5)=0$
B1 1
cao
23. Let $x$ represent the number of defective articles
$\therefore X \sim B(10,0.032)$
(a) $\mathrm{P}(X=2)=10 \nearrow_{2}^{45}(0.032)^{2}(1-0.032)^{\mathrm{p}}$

Use of ${ }^{n} C_{r} p^{r} q^{n-5}$ All correct

$$
=\underline{0.0355234 \ldots}
$$

A1 3
AWRT 0.0355
(b) Large n , small $\mathrm{p} \Rightarrow$ Poisson approximation B1 seen or implied
with $\lambda=100 \times 0.032=3.2$

$$
\begin{aligned}
& \mathrm{P}(X<4)=\mathrm{P}(X \leq 3)=\mathrm{P}(0)+\mathrm{P}(1)+\mathrm{P}(2)+\mathrm{P}(3) \\
& P(X \leq 3) \text { stated or implied } \\
& =e^{-3.2}\left\{1+3.5+\frac{(3.2)^{2}}{2}+\frac{(3.2)^{3}}{6}\right\} \\
& \text { All correct } \\
& \quad \underline{\text { NB Normal Approx } \Rightarrow \frac{0}{4}} \\
& =\frac{0.602519 \ldots}{\text { AWRT } 0.603}
\end{aligned}
$$

(c) $n p \& n q$ both $>5 \Rightarrow$ Normal approximation

M1
NApprox
With $n p=32$ and $n p q=30.976$ A1
Both
$\mathrm{P}(X>42) \approx \mathrm{P}(Y>42.5)$ where $Y \sim N(32,30.976)$
Standard
$=\mathrm{P}\left(Z>\frac{42.5-32}{\sqrt{30.976}}\right)$
their $n p, \sqrt{n p q}$
All correct
$=P(Z>1.8865 \ldots)$
AWRT 1.89
$=\underline{0.0294}$
$0.0294-0.0297$
24. Let $X$ represent number of accidents/month $\therefore X \sim \mathrm{P}_{0}$ (3) B1
(a) $\mathrm{P}(X>4)=1-\mathrm{P}(X \leq 4) ;=1-0.8513=\underline{0.1847}$ M1; A1 3
(b) Let $Y$ represent number of accidents in 3 months
$\therefore Y \sim P_{0}(3 \times 3=9)$ B1

Can be implied
$\mathrm{P}(Y>4)=1-0.0550=\underline{0.9450}$
B1 2
(c) $\mathrm{H}_{0}: \lambda=3 ; \mathrm{H}_{1}: \lambda<3$

B1
both
$\alpha=0.05$
$\mathrm{P}(X \leq 1 / \lambda=3)=0.1991 ;>0.05$
B1 M1
$\therefore$ Insufficient evidence to support the claim that the mean number of accidents has been reduced.

A1ft 4
(NB: CR: $X \leq 0 ; X=1$ not in CR; same conclusion $\Rightarrow \mathrm{B} 1, \mathrm{M} 1, \mathrm{~A} 1$ )
(d) $\mathrm{H}_{0}: \lambda 24 \times 3=72 ; \mathrm{H}_{1}: \lambda<72$

B1
can be implied $\lambda=72$
$\alpha=0.05 \Rightarrow \mathrm{CR}: \delta<-1.6449$
B1 B1
both $H_{0} \& H_{1}$
-1.6449
Using Normal approximation with $\mu=\sigma^{2}=72$
Can be implied
$\delta=\frac{55.5-72}{\sqrt{72}}=-1.94454 \ldots$
Stand. with $\pm 0.5, \mu=\sigma$
AWRT-1.94/5
Since $-1.944 \ldots$ is in the CR, $\mathrm{H}_{0}$ is rejected.
A1ft 7
There is evidence that the restriction has reduced the number of accidents

Context \& clear evidence

Aliter (d)
$p=0.0262<0.05$
AWRT 0.026 equn to -1.6449
25. (a) Fixed no of trials/ independent trials/ success \& failure/ Probab of success is constant any 2
(b) $\quad X$ is rv 'no of defective components $X \sim \operatorname{Bin}(20,0.1)$
(c) $\mathrm{P}(X=0)=0.1216$
$=0,0.1216$
(d) $\mathrm{P}(X>6)=1-\mathrm{P}(X \leq 6)=1-0.9976=0.0024$

Strict inequality \& 1- with $6 s, 0.0024$
(e) $\mathrm{E}(X)=20 \times 0.1=2$ B1
$\operatorname{Var}(X)=20 \times 0.1 \times 0.9=1.8$
B1 2
(f) $\quad X \sim \operatorname{Bin}(100,0.1)$
Implied by approx used
$X \sim \mathrm{P}(10)$ B1
$\mathrm{P}(X>15)=1-\mathrm{P}(X \leq 15)=1-0.9513=0.0487$ M1A1 Strict inequality and 1 - with $15,0.0487$
( $\mathbf{O R} X \sim N(10,9), P(X>15.5)=1-P(Z<1.83)$
$=0.0336$ (0.0334) with 15.5
B1M1A1)
$(\mathbf{O R} X \sim N(10,10), P(X>15.5)=1-P(Z<1.74)$
$=0.0409$ ( 0.0410 ) with 15.5
BlM1A1) 4
26. (a) A range of values of a test statistic such that if a value of the test statistic obtained from a particular sample lies in the critical region, then the null hypothesis is rejected (or equivalent).
(b) $\quad \mathrm{P}(X<2)=\mathrm{P}(X=0)+\mathrm{P}(X=1)$
both M1
$=e^{-\frac{1}{7}}+\frac{e^{\frac{1}{7}}}{7}$
$=0.990717599 \ldots=0.9907$ to 4 sf
both A1
A1 3
awrt 0.991
$X \sim \mathrm{P}\left(14 \times \frac{1}{7}\right)=\mathrm{P}(2)$
$\mathrm{P}(X \leq 4)=0.9473$
M1A1
3
Correct inequality, 0.9473
$\mathrm{H}_{0}: \lambda=4, \mathrm{H}_{1}: \lambda<4$ B1B1

Accept $\mu \& H_{0}: \lambda=\frac{1}{7}, H_{1}: \lambda<\frac{1}{7}$
$X \sim \mathrm{P}(4)$
Implied
$\mathrm{P}(X \leq 1)=0.0916>0.05$, M1A1 Inequality 0.0916

So insufficient evidence to reject null hypothesis
Number of breakdowns has not significantly decreased

A1
A1 7
27. (a) No of defects in carpet area $a$ sq m is distributed $\operatorname{Po}(0.05 a)$

B1B1
Poisson, 0.05a
Defects occur at a constant rate, independent, singly, randomly B1 3
Any 1
(b) $\quad X \sim \mathrm{P}(30 \times 0.05)=\mathrm{P}(1.5)$

B1
$\mathrm{P}(X=2)=\frac{e^{-1.5} \times 1.5^{2}}{2}=0.2510$
M1A1 3
Tables or calc 0.251(0)
(c) $\mathrm{P}(X>5)=1-\mathrm{P}(X \leq 5)=1-0.9955=0.0045$

M1M1A1 3
Strict inequality, 1-0.9955, 0.0045
(d) $\quad X \sim \mathrm{P}(17.75)$

B1
Implied
$X \sim \mathrm{~N}(17.75,17.75) \quad$ B1
Normal, 17.75
$\mathrm{P}(X \geq 22)=\mathrm{P}\left(Z>\frac{21.5-17.75}{\sqrt{17.75}}\right)$
M1M1

Standardise, accept 22 or $\pm 0.5$

$$
=-\mathrm{P}(Z>0.89)
$$

awrt 0.89
$=0.1867$
A1 6

M1A1 2
Require 1 minus and correct inequality
(b) $\mathrm{P}(S \leq 1)=\mathrm{P}(S=0)+\mathrm{P}(S=1), e^{-2.71}+2.71 e^{-2.71},=0.2469 \quad$ M1,A1,A1 3
awrt 0.247
(c) $\mathrm{P}(\mathrm{T} \leq 18)=\mathrm{P}(\mathrm{Z} \leq-1.4)=0.0808$
$4 d p, c c$ no marks
28. (a) $\mathrm{P}(R \geq 4)=1-\mathrm{P}(R \leq 3)=0.6533$

M1,A1 2
29. (a) $n$ large, $p$ small

B1,B1
B1
$X \sim \mathrm{~B}\left(12, \frac{1}{150}\right)$
Implied
$\mathrm{P}(X=2)=\mathrm{C}_{2}^{12}\left(\frac{1}{150}\right)^{2}\left(\frac{149}{150}\right)^{10},=0.027$
M1A1,A1
4

Use of Bin including $C_{2}^{12}, 0.0027(4)$ only
(c) $\quad X \sim \operatorname{Po}(n p)=\operatorname{Po}(8)$

B1,B1
Poisson, 8
$\mathrm{P}(X<7)=\mathrm{P}(X \leq 6)=0.3134$
$X \leq 6$ for method, 0.3134
30. (a) Vehicles pass at random / one at a time / independently / at a constant rate Any 2\&context

B1B1dep 2
(b) $X$ is the number of vehicles passing in a 10 minute interval,
$X \sim \operatorname{Po}\left(\frac{51}{60} \times 10\right)=\operatorname{Po}(8.5)$
Implied Po(8.5)
$\mathrm{P}(X=6)=\frac{8.5^{6} \mathrm{e}^{-8.5}}{6!},=0.1066($ or $0.2562-0.1496=0.1066)$
M1A1 3
Clear attempt using 6, 4dp
(c) $\mathrm{P}(X \geq 9)=1-\mathrm{P}(X \leq 8)=0.4769$

M1A1 2
Require 1 minus and correct inequality
(d) $\mathrm{H}_{0}: \lambda=8.5, \mathrm{H}_{1}: \lambda<8.5$

B1ft,B1ft
One tailed test only for alt hyp
$\mathrm{P}(X \leq 4 \mid \lambda=8.5)=0.0744,>0.05$ M1A1
$X \leq 4$ for method, 0.0744
(Or $\mathrm{P}(X \leq 3 \mid \lambda=8.5)=0.0301,<0.05$ so CR $X \leq 3$ correct CR
Insufficient evidence to reject $\mathrm{H}_{0}$, 'Accept' M1 so no evidence to suggest number of vehicles has decreased. Context A1ft
31. (a) $\lambda$ is large or $\lambda>10$
(b) $\quad Y \sim \mathrm{~N}(30,30)$ may be implied
$\mathrm{P}(Y>28)=1-\mathrm{P}(Y \leq 28.5)$
$=1-\mathrm{P}\left(Z \leq \frac{28.5-30}{\sqrt{30}}\right)$
$=1-\mathrm{P}(Z \leq-0.273)$
completely correct
$=\underline{0.606-0.608}$
must be 3 or $4 d p$
32. (a) $\operatorname{Po}(1)$

B1 B1
Each patient seen singly
or patients with disease seen randomly
or patients seen at constant rate
or each patient assumed independent of the next
B1
3
(b) $\quad X \sim \operatorname{Po(4)~may~be~implied~} \quad$ B1
$\mathrm{P}(X>3)=1-\mathrm{P}(X \leq 3) \quad$ M1
$=1-0.4335$ A1
$=\underline{0.5665} \quad \mathrm{~A} 1$
4
(c) $\mathrm{H}_{0}: \lambda=6$

B1
$\mathrm{H}_{1}: \lambda<6$ B1
$\mathrm{P}(X \leq 2)=0.0620 \quad \alpha=0.05 \Rightarrow$ critical region $X \leq 1$
$0.0620>0.05 \quad 2$ not in critical region M1 A1

M1
The number of patients with the disease seen by the doctor has not been reduced

A1 6
(d) This does not support the model as the disease will occur in outbreaks; the patients seen by the doctor are unlikely to be independent of each other/don't occur singly

B1; B1 2
33. (a) Weeds grow independently, singly, randomly and at a constant rate
(weeds $/ \mathrm{m}^{2}$ )
any 2
B1 B1 2
(b) Let $X$ represent the number of weeds $/ \mathrm{m}^{2}$
$X \sim \operatorname{Po}(0.7)$, so in $4 \mathrm{~m}^{2}, \lambda=4 \times 0.7=2.8 \quad$ B1
$\mathrm{P}(Y<3)=\mathrm{P}(Y=0)+\mathrm{P}(Y=1)+\mathrm{P}(Y=2)$ M1
$=\mathrm{e}^{-2.8}\left(1+2.8+\frac{2.8^{2}}{2}\right)$
$=0.46945$
(c) Let $X$ represent the number of weeds per $100 \mathrm{~m}^{2}$
$X \sim \operatorname{Po}(100 \times 0.7=70)$
$\mathrm{P}(X>66) \approx \mathrm{P}(Y>66.5)$ where $Y \sim \mathrm{~N}(70,70)$

A1 6
34.

(a) $\mathrm{P}(X<-4.2)=\frac{0.8}{10}=0.08$

B1 1
(b) $\mathrm{P}(|X|<1.5)=\frac{3}{10}=0.3$

M1 A1 2
(c) $\quad Y=$ no. of lengths with $|X|<1.5 \quad \therefore Y \sim \mathrm{~B}(10,0.3)$
$\mathrm{P}(Y>5)=1-\mathrm{P}(Y \leq 5) \quad$ M1
$=1-0.9527 \quad 0.0473 \quad \mathrm{~A} 1$
$R=$ no. of lengths of piping rejected
$R \sim \mathrm{~B}(60,0.08) \Rightarrow R \approx \sim \operatorname{Po}(4.8) \quad 4.8$ or $60 \times(a)$
B1 ft
$\mathrm{P}(R \leq 2)=\mathrm{e}^{-4.8}\left[1+4.8+\frac{(4.8)^{2}}{2!}\right] \quad$ Po and $\leq 2$, formula $\quad$ M1, M1 A1 ft
( $f t$ for their $\lambda$ if full expression seen)
$=17.32 \times \mathrm{e}^{-4.8}=0.1425 \ldots$
(accept awrt 0.143) A1 cao5
35. (a) $X=$ no. of customers arriving in 10 minute period
$X \sim \operatorname{Po}(3) \quad \mathrm{P}(X \geq 4)=1-\mathrm{P}(X \leq 3)=, \quad 1-0.6472=0.3528 \quad$ M1 A1
(b) $\quad Y=$ no. of customers in 30 minute period $Y \sim \operatorname{Po(9)}$
$\mathrm{P}(Y \leq 7)=0.3239$
B1
M1 A1 3
(c) $\quad p=$ probability of no customers in 5 minute period $=\mathrm{e}^{-1.5}$

B1
$C=$ number of 5 minute periods with no customers
$C \sim \mathrm{~B}(6, p) \quad$ M1
$\mathrm{P}(C \leq 1),=(1-p)^{6}+6(1-p)^{5} p$
M1, M1 A1 $=0.59866 \ldots$
(accept awrt 0.599)
(d) $\quad W=$ no. of customers on Wednesday morning

| $3 \frac{1}{2}$ hours $=210$ minutes $\quad \therefore W \sim \operatorname{Po}(63)$ | '63' | B1 |
| :--- | :--- | ---: |
| Normal approximation | $W \approx \sim \mathrm{~N}\left(63,(\sqrt{ } 63)^{2}\right)$ |  |
| $\mathrm{P}(W>49) \approx \mathrm{P}(W \geq 49.5)$ | M1 A1 |  |
|  |  | $\pm \frac{1}{2}$ |
|  | M1 |  |

$$
\begin{array}{rlr}
= & \mathrm{P}\left(Z \geq \frac{49.5-63}{\sqrt{63}}\right) & \\
& \text { standardising } & \mathrm{M} 1 \\
= & \mathrm{P}(Z \geq-1.7008) & \mathrm{A} 1 \\
= & 0.9554 \text { (tables) } & \\
& \text { (accept awrt } 0.955 \text { or } 0.956) & \mathrm{A} 17
\end{array}
$$

1. This question was well answered by the majority of candidates with many scoring full marks. There were, of course, candidates who failed to score full marks. This was usually the result of inaccurate details, rather than lack of knowledge. In particular, manipulation of inequalities requires concentration and attention to detail. In part (a) the most common error seen was using $P(X=3)=P(X \leq 4)-P(X \leq 3)$.

Parts (b) and (c) were usually correct. The most common error was to find $\mathrm{P}(X \leq 3)$ rather than $\mathrm{P}(X \leq 4)$ in part (b). A minority of candidates used the Normal as their approximation in part (d). The simple rule " $n$ is large, $p$ is small: use Poisson" clearly applies in this case.
2. The majority of candidates were familiar with the technical terms in part (a), but failed to establish any context.

Part (b) was a useful source of marks for a large proportion of the candidates. The only problems were occasional errors in detail. In part (i) a few did not spot the change in time scale and used $\mathrm{Po}(4)$ rather than $\mathrm{Po}(8)$. Some were confused by the wording and calculated $\mathrm{P}(X=8)$ rather than $\mathrm{P}(X=0)$. The main source of error for (ii) was to find $1-\mathrm{P}(X \leq 4)$ instead of $1-\mathrm{P}(X \leq 3)$.

In part (c) the Normal distribution was a well-rehearsed routine for many candidates with many candidates concluding the question with a clear statement in context.
The main errors were

- Some other letter (or none) in place of $\lambda$ or $\mu$
- Incorrect Normal distribution: e.g. $\mathrm{N}(60,60)$
- Omission of (or an incorrect) continuity correction
- Using 48 instead of 60
- Calculation errors

A minority of candidates who used the wrong distribution (usually Poisson) were still able to earn the final two marks in the many cases when clear working was shown. This question was generally well done with many candidates scoring full marks.
3. Although there were a minority of candidates who were unable to identify the correct distribution to use the majority of candidates achieved full marks to parts (a) (b) and (c). Part (d) seemed to cause substantial difficulty. In part (a) the majority of candidates identified that a Poisson (rather than the Binomial) distribution was appropriate but some calculated the parameter as 2.5 or 4 rather than 0.4 . A few used $\operatorname{Po}(1)$ and calculated $\mathrm{P}(Y=5)$.
In part (b) and part (c) the most common error was to use Po(2.5). The majority of candidates were able to work out $\mathrm{P}(X>1)$ and $\mathrm{P}(X=2)$ using the correct Poisson formula. Many thought that their answer to part (c) was the correct solution while others used or multiplied their answers to both (b) and (c). Whether stating a correct or incorrect solution only a minority used the statistical term "independence" as the reason for their answer.
4. This question was accessible to the majority of candidates, with many gaining full marks. Most recognised the need to use a Poisson distribution in part (a) and translated the time of one hour successfully to a mean of 10 . Common errors included using a mean of 6 or misinterpreting $\mathrm{P}(X$ $<9)$ as $\mathrm{P}(X \leq 9)$ or using $1-\mathrm{P}(X \leq 8)$. In part (b), a high percentage of candidates gained full marks for using a Normal approximation with correct working. Marks lost in this part were mainly due to using a 49.5 instead of 50.5 or no continuity correction at all. A small number of candidates wrote the distribution as $\mathrm{B}(240,1 / 6)$ and translated this to $\mathrm{N}(40,100 / 3)$.
5. Part (a) was answered well with the majority of candidates gaining full marks.

Part (b) was also a good source of marks for a large majority of the candidates. Common errors included using 23.9...for variance and 19.5 instead of 20.5. A sizeable minority of candidates used 21.5 after applying the continuity correction. A few candidates had correct working up to the very end when they failed to find the correct probability by not subtracting the tables’ probability from 1.
6. Parts (a) and (b) were completed successfully by most candidates. The most common errors seen were using the wrong Poisson parameter or identifying the incorrect probability in part (b).

Part (c) proved to be a good discriminator with only those with good mathematical skills able to attain all the marks for this part of the question. Few candidates used the method given on the mark scheme and chose to use natural logarithms instead. Whilst this is an accepted method this knowledge is not expected at S2 and full marks were gained by the most able candidates using the given method.

In part (d) a few candidates seemed confused by this with some using 1.7 or $2 / 15$ as a probability rather than the 0.8 given in the question, and far too many seemed unable to use 60 p and $£ 1.50$ correctly when calculating the profit.
7. This question proved to be a good start to the paper for a majority of the candidates. There were many responses seen which earned full marks.

The most common errors in parts (a) and (b) concerned the routine manipulation of inequalities. In part (a) $1-\mathrm{P}(X \leq 1)$ was often seen and in (b), while most candidates agreed that
$\mathrm{P}(5 \leq X \leq 6)$ was the required probability, with many then choosing the standard technique of $\mathrm{P}(X \leq 6)-\mathrm{P}(X \leq 4)$, there were candidates who proceeded with a variety of methods. Incorrect expressions such as $\mathrm{P}(X \leq 6)-\mathrm{P}(X \leq 4)$ were seen not infrequently. A correct but inefficient method which was commonly used included:
$\mathrm{P}(X=5)+\mathrm{P}(X=6)=(\mathrm{P}(X \leq 6)-\mathrm{P}(X \leq 5))+(\mathrm{P}(X \leq 5)-\mathrm{P}(X \leq 4))$
Part (c) was poorly answered. There were a significant minority of candidates who obtained a 'correct' answer for the mean in part (c), but who nevertheless lost the mark because their answer was not written, as instructed, correct to 2 decimal places. Many candidates were unable to calculate the variance. There were a variety of incorrect formulae used.

The general response to (d) was good, although many candidates simply gave the response that is appropriate for a more frequent type of question on the Poisson distribution requiring comment: ("singly/independently/randomly/constant rate").

Part (e) was particularly well done. Even the minority who struggled, or even omitted, some of the earlier parts of the question were able to gain both marks in part (e).
8. This question was generally answered well. A few candidates put the Poisson for (a) and then used Variance $=$ Mean to got 5.5 for the variance. Some candidates rounded incorrectly giving an answer of 5.49 for the variance.
Part (c) was generally answered correctly although a minority of candidates used the normal approximation - most used 2.5 in their standardisation and so got 1 mark out of the 4 .
9. Part(a) was done well generally although a reference to 'calls' was not made by a few candidates. Weak candidates talked about the Poisson needing large numbers and others seemed to not understand what was required at all; writing ‘quick and easy’. Part (b) was done correctly by the majority of candidates. A few did not use $\mathrm{Po}(4.5)$ in (i) and a number used $\mathrm{P}(X>8)=1-$ $\mathrm{P}(X \leq 7)$ in (ii).In part (c) weaker candidates did not use $\lambda$ for their hypotheses nor did they use $\operatorname{Po}(9)$. Some hypotheses had $\lambda=3.5$ and $\lambda \geq 3.5$. Two tail tests were often suggested. Most candidates got to 0.0739 and only a few candidates used the critical value route. Only the able candidates got the interpretation of the significance test correct. Weak candidates generally only considered whether it was significant or not, with mixed success. They rarely managed to interpret correctly in context.
10. Most candidates were able to attempt part (b) successfully as these were fairly standard calculations. However, when required to apply Poisson probabilities to a problem it was only the better candidates who attained any marks in part (c).
(a) A sizeable proportion of candidates, whilst having learnt the conditions for a Poisson distribution, failed to realise that this applied to the events occurring. There were references to 'trials' and 'things' in some solutions offered.
(b) (i) Most candidates recognised $\mathrm{Po}(6)$ and were able to answer this successfully, either from the tables or by calculation. Common errors were using incorrect values from the table or calculating the exact value incorrectly.
(ii) Although many candidates attained full marks for this part, some were unable to express 'at least 5' correctly as an inequality and used $\mathrm{P}(X \leq 5)$.
(c) Many of the successful candidates used a $\mathrm{Po}(3)$ to give a correct solution. Of the rest most candidates failed to realise that there were two ways for exactly one vehicle to pass the point and so only performed one calculation. This was often for $\mathrm{P}(1 \mathrm{car})$ and $\mathrm{P}(1$ other vehicle), which were then added together. However there were some candidates who gained the correct answer via this method.
11. This question was quite well done. Most candidates were aware of the conditions for a Poisson distribution but many lost marks as they did not answer the question in context, although the examination question actually specified this. A few did not realise that independent and random were the same condition. Cumulative probability tables were well used in part (c) and there were many accurate solutions using the Poisson formula.
Most candidates used a mean of 4.5 in part (d) and there were many accurate results.
12. This question was accessible to most candidates. Parts (a), (d) and (e) were generally well answered with a small proportion of candidates using $\operatorname{Po}(10)$ in part (d) and thus quoting that the mean and variance were the same. Part (b) caused a few problems as some used $\operatorname{Po}(0.1)$ and found $\mathrm{P}(X=2)$ or used $X \sim \mathrm{~B}(2,0.1)$. In part (c) some candidates still did not correctly use $\mathrm{P}(X>1)=1-\mathrm{P}(X<1)$. A similar mistake occurred in part (e) where they used $\mathrm{P}(X>6)=1-\mathrm{P}(X \leq 6)$.
Candidates need to be reminded of the rubric on the front of the question paper. It does say 'appropriate degrees of accuracy'. Many rounded too early and did not realise that an answer to 1 sf is not accurate enough. Answers of 0.001 were common in part (c)
13. This was usually completely correct with very few errors.
14. It was disappointing to find that a large number of candidates failed to attain both of the first 2 marks available. These were often the only marks lost by some, since the majority of candidates achieved most or all marks. In part (d) most candidates did attempt an approximation, although a minority calculated an exact binomial. Again, the common errors were to fail to use a continuity correction and the standard deviation when using the approximation and then not using the $1-\Phi(z)$. The simple calculation of 16 x the answer to part (d) was performed correctly by the majority of candidates attempting this part of the question. A common error was to attempt a binomial probability.
15. The majority of candidates knew the conditions for the Poisson distribution but many did not get the marks because they failed to put them into context. As in many previous series, it was very common for candidates to repeat at least some of these conditions parrot-fashion preceded by "events occur" or "it occurs". Other common errors were listing randomness and independence as separate reasons and citing the fixed time period and lack of an upper limit as reasons. Quite a number failed to mention the parameter for the distribution. The majority of candidates answered part (b) correctly. Most candidates answered part (c) correctly. Where marks were lost it was usually through failing to use a continuity correction rather than applying it wrongly.
16. Most candidates answered Part (a) correctly. A small number of candidates calculated the probability for less than or equal to 3 although a minority thought that dividing by 0 ! in $\mathrm{P}(X=0)$ gave zero. In part (b) carrying out the hypothesis test was more challenging though there was clear evidence that candidates had been prepared for this type of question. However, using $p$ instead of $\lambda$ or $\mu$, when stating the hypotheses, was often seen and incorrectly stating H 1 as $\lambda>$ 1.25 or 5 also lost marks. Many candidates calculated $\mathrm{P}(\mathrm{X} \leq 11)$ instead of looking at $\mathrm{P}(\mathrm{X} \geq 11)$. A diagram would have helped them or the use of the phrase "a result as or more extreme than that obtained". Those who used the critical region approach made more errors. Some candidates correctly calculated the probability and compared it with 0.025 but were then unsure of the implications for the hypotheses. A few candidates used a 2-tailed hypothesis but then used 0.05 rather than 0.025 in their comparison. Most candidates gave their conclusions in context.
17. This was well answered by almost all candidates and many correct solutions were seen. A few candidates tried to use Poisson rather than Binomial for parts (a) and (b). In part (b) a few candidates used $B(10,0.6)$ instead of $B(10,0.06)$. In part (c)(i) most errors occurred because candidates did not understand what was meant by "between 10 and 13 inclusive" The most common wrong answer was in using $\mathrm{P}(10 \leq X \leq 13)=\mathrm{P}(X \leq 13)-\mathrm{P}(X \leq 10)$ instead of $\mathrm{P}(\mathrm{X} \leq$ $13)-\mathrm{P}(X \leq 9)$ Another fairly common error was using $\mathrm{P}(X \leq 13)-(1-\mathrm{P}(X \leq 10))$ Some candidates tried to use a continuity correction in this Poisson approximation. Part (c)(ii) was often correct the most common errors being to use 7.5 instead of 7.05 for the variance and to use an incorrect continuity correction.
18. Many candidates did well on this question and gained all 9 marks.

In part (a) nearly all candidates realised the Poisson distribution was appropriate but not all stated the parameter of 1.5 . Often this was stated in part $b$ which did not gain the marks.

In part (c) many candidates used a Poisson distribution with a parameter of 4.5 rather than cubing the probability of $\mathrm{X} \geq 1$ from a Poisson 1.5.

Part (d) was done very well by all candidates; the main error being the statement
$\mathrm{P}(\mathrm{X}>4)=1-\mathrm{P}(\mathrm{X} \leq 3)$
19. Most candidates correctly used a $\operatorname{Po}(3)$ distribution although a significant minority attempted to used a Normal distribution. The most common error was using $\mathrm{P}(\mathrm{X}>7)=1-\mathrm{P}(\mathrm{X} \leq 6)$
20. Many candidates did not achieve any marks in part (a) as they failed to give conditions in context, events being the most common error seen. Part (b) was done well and if candidates lost a mark then it was usually the final mark due to accuracy. A common answer was 0.082 . Part (c) was generally completed satisfactorily, but there were a number of candidates who struggled with the inequalities. A common error was $P(Y>7)=1-P(T \leq 6)$. Diagrams were again in evidence; these candidates were perhaps the least likely to make mistakes with the inequalities. Some candidates calculated a probability using $\mathrm{P}(2.5)$ and then squared their answer. The overall response to part (d) was good. However, only a minority scored full marks. Most candidates failed to implement the instruction to write their answer "to 2 decimal places". There were other errors; omission of the continuity correction or the wrong version (40.5), confusion between variance and standard deviation, and problems dealing with a negative $z$-value.
21. The overall response was good, with a large number of candidates scoring at least five out of the seven marks. However, a small number of candidates chose to ignore the instructions to "use a suitable approximation". Most candidates were familiar with the conditions required for the Poisson approximation to the Binomial in part (a). However, a small number of candidates quoted this correct reason, but used this as justification for a Normal approximation. Not all candidates using the Poisson distribution earned the second mark. A final answer of 0.156 was fairly common, particularly amongst those who had used the Poisson formula rather than the cumulative tables.

The response to part (b) was excellent. There were a large number of perfect answers. A small number of candidates ignored the instruction to approximate and continued the use the Binomial
distribution. Cumulative tables are not available for this particular distribution, so candidates calculated five separate probabilities using the Binomial formula and then added, resulting in many of them able to obtain the correct answer using this method.
22. Candidates knew how to answer parts (a) and (b) but many did not work to sufficient accuracy. If they used their calculator instead of the tables they were expected to give their answer to the same accuracy as the tables. Too many of them did not read part(c) carefully enough. The random variable $T$ was defined to be normally distributed and thus $\mathrm{P}(T=5)=0$.
23. This question was a good source of marks for many of the candidates, with many of them gaining full marks. For those that did not gain full marks, the common errors were premature approximation; wrong interpretation of 'fewer than 4 ';ignoring the continuity correction and in part (c) using a Poisson approximation and then a normal approximation to this Poisson approximation.
24. For those candidates that could interpret 'more than 4 accidents occurred' correctly parts (a) and (b) were a good source of marks. Part (b) was often well answered and many candidates gained full marks. In part (c) incorrect hypotheses and ignoring the continuity correction were the common errors coupled with poor use of the appropriate significance test. Candidates need to have a simple algorithm at their fingertips to deal with tests of significance.
25. This was a good source of marks for a large majority of candidates. Many were able to write down two conditions for a Binomial distribution, with some writing down all four conditions for good measure. However some candidates muddled up the concepts of trial, event and outcome. The response of 'a fixed number of events' was given no credit. Parts (b), (c), (d) and (e) were usually well answered. In part (f), successful candidates either applied a Po (10) or a N(10, 9) approximation. Some of the candidates who used the $N(10,9)$ approximation did not apply the correct continuity correction.
26. In part (a) many candidates struggled to explain the concept of a critical region, although some gave a correct definition as the range of values where the null hypothesis is rejected. Many correct solutions were seen for parts (b) and (c). However the weaker candidates were not able to translate the concept 'at most 4 breakdowns' to the correct inequality. In part (d), as with Q3, many candidates successfully performed the required hypothesis test using a probability method. Again, there was a sizeable number of candidates who incorrectly found $P(X=1)$ and compared this probability with the significance level. Again, a minority of candidates decided to approach this question using the critical region strategy. Marks were lost if candidates did not give evidence of their chosen critical region.
27. This was a well answered question and high marks were frequently being scored. In part (a), many candidates chose the correct Poisson model and gave a correct reason in the light of the problem posed. Many correct solutions were seen in parts (b) and (c). In part (d), many candidates found the correct Normal approximation to the Poisson distribution. The most common error was the incorrect application of the continuity correction with weaker candidates generally losing the final two accuracy marks. In part (a), a small minority of candidates incorrectly chose a Binomial model and applied this model throughout the question, thereby losing a considerable number of marks.
28. The whole question was generally very well answered, by far the most common error was the use of a continuity correction in part (c). A small number of candidates didn't realise that part (b) required the sum of two probabilities.
29. This was a well answered question with many candidates scoring full marks. In part (a), many candidates realised the conditions of a large value of $n$ and a small value of $p$ when approximating the Binomial Distribution by the Poisson distribution. One common error in part (b) was for candidates to apply the Poisson approximation when the number of trials was only twelve, even though these candidates were able to write down the appropriate conditions in part (a).
30. Candidates were able to express two conditions for a Poisson distribution in context with vehicles passing by a particular point on the road. Many candidates then answered part (b) and (c) correctly. In part (d) a majority of candidates was able to give a full solution by either using a probability or critical region approach to their hypothesis test.
31. This question was generally well answered with many candidates gaining full marks. In part (b) a minority of candidates standardized correctly but then found the incorrect area.
32. This question was well answered with many candidates gaining 14 or 15 marks. In part (a) most candidates spotted the Poisson distribution but few related their reason to the context of the question. In part (d) the majority of candidates realized that the Poisson was no longer appropriate, but some failed to give a reason which related the breakdown of one of the Poisson conditions to the context of the question.
33. Most candidates scored well on this question, but too many lost marks in part (a) by not giving their answer in context. Too many candidates lost a mark by not answering part (b) to the required level of accuracy. Candidates were obviously more at ease in part (c) where they were able to leave the answer as they found it from tables.
34. No Report available for this question.
35. No Report available for this question.

